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# MEDICAL AND BIOLOGICAL PHYSICS

Edited by Prof. A. Chalyi

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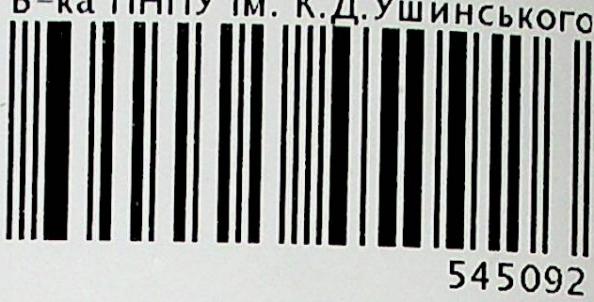
# **MEDICAL AND BIOLOGICAL PHYSICS**

**Edited by Prof. Alexander V. Chalyi**

*Recommended by the Ministry of Health Care of Ukraine  
as a textbook for the students of higher medical  
establishments of the IV accreditation level*

**Fourth edition**

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for the students of higher medical establishments of the IV accreditation level  
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The book is aimed at elucidating the most important aspects of the medical and biological physics in accordance with the program asserted by the Ministry of Health Care of Ukraine, and written for the students of higher medical institutions as well as for teachers, scientific researchers and all those readers interested in modern problems of the medical and biological physics.

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